

Reference angles and evaluating higher trig angles with Trig 1-2-3

**Create the two reference triangles and the unit circle picture below:**

You should know how to evaluate all of the following trig values using the above pictures:

$\sin 0^\circ =$	$\sin 30^\circ =$	$\sin 45^\circ =$	$\sin 60^\circ =$
$\cos 0^\circ =$	$\cos 30^\circ =$	$\cos 45^\circ =$	$\cos 60^\circ =$
$\tan 0^\circ =$	$\tan 30^\circ =$	$\tan 45^\circ =$	$\tan 60^\circ =$

$\sin 90^\circ =$	$\sin 180^\circ =$	$\sin 270^\circ =$	$\sin 360^\circ =$
$\cos 90^\circ =$	$\cos 180^\circ =$	$\cos 270^\circ =$	$\cos 360^\circ =$
$\tan 90^\circ =$	$\tan 180^\circ =$	$\tan 270^\circ =$	$\tan 360^\circ =$

Now you need to learn how to find reference angles:

**If you have a first quadrant angle, the angle is the reference angle.****If you have a second quadrant angle, the reference angle is found by  $180 - \theta$** **If you have a third quadrant angle, the reference angle is found by  $\theta - 180$** **If you have a fourth quadrant angle, the reference angle is found by  $360 - \theta$** Find the reference angle of the following angles  $\theta$ :

$30^\circ =$	$150^\circ =$	$210^\circ =$	$330^\circ =$
$45^\circ =$	$135^\circ =$	$225^\circ =$	$315^\circ =$
$60^\circ =$	$120^\circ =$	$240^\circ =$	$300^\circ =$

Hopefully you see how you are able to find sin, cos, and tan of these angles also without a calculator (but you can always verify)

**Trig 1-2-3** is the process VC math teachers show students how to evaluate these other angles:

Step 1: Determine if the trig value of the angle is positive or negative (using unit circle picture)

Step 2: Rewrite the trig function

Step 3: Find the reference angle (**you are now ready to evaluate what you have**)

Example:  $\sin 225^\circ = -\sin 45^\circ = -\frac{\sqrt{2}}{2}$

**Evaluate the following angles using Trig 1-2-3**

$\sin 120^\circ =$	$\sin 135^\circ =$	$\sin 150^\circ =$	$\sin 210^\circ =$
$\cos 120^\circ =$	$\cos 135^\circ =$	$\cos 150^\circ =$	$\cos 210^\circ =$
$\tan 120^\circ =$	$\tan 135^\circ =$	$\tan 150^\circ =$	$\tan 210^\circ =$

$\sin 225^\circ =$	$\sin 240^\circ =$	$\sin 300^\circ =$	$\sin 315^\circ =$
$\cos 225^\circ =$	$\cos 240^\circ =$	$\cos 300^\circ =$	$\cos 315^\circ =$
$\tan 225^\circ =$	$\tan 240^\circ =$	$\tan 300^\circ =$	$\tan 315^\circ =$

$\sin 330^\circ =$
$\cos 330^\circ =$
$\tan 330^\circ =$

Angles higher than  $360^\circ$  can be found by doing one addition step: **Find the coterminal angle between  $0^\circ$  and  $360^\circ$ .**

Example:  $\cos 660^\circ = \cos 300^\circ$  (since  $660 - 360 = 300$ )  $= +\cos 60^\circ = \frac{1}{2}$

**You try some of these mixed problems:**

$\sin 570^\circ =$	$\tan -240^\circ =$	$\cos 675^\circ =$	$\sin -210^\circ =$
$\cos 600^\circ =$	$\tan -315^\circ =$	$\sin -60^\circ =$	$\cos 855^\circ =$

